

THE GEOMETRICAL KEY: OR

The Gate of Equations Unlocked.

A New Discovery of the Constructions of all Equations howsoever affected, not exceeding the 4th degree; viz. Of *Linears*, *Quadratics*, *Cubics*, and *Biquadratics*, and the finding of all their Roots as well true as negative, without the use of *Mesolabe*, and *Trisection of Angles*; without Reduction, Depression, or any other previous preparation of Equations, by a Circle and any (and that but one only) *Parabole*: and this by one only general Rule, than which a more simple, more perfect, more general, more easy to be understood, or more fit for practise, cannot be devised or wished for. Fortified with Demonstrations, Illustrated with Figures to each Equation, and Exemplified with numeral Equations (according to all the varieties of Cases) adapted to each Figure, for the use of young Mathematicians: a work hitherto desired.

By THOMAS BAKER, Rector of Bishop Nympton.



He Treatise consists of about a Quire of Paper, the Discourse whereof (but not the *Algebraick Calculus*) is both in *Latin* and *English*, the better to promote its forreign vend; and this doth not render it above three Sheets the larger than it would have been in one of these Languages. Besides which, there is belonging to it diverse Draughts of Schemes to be engraven, and one *Folio* Draught, wherein the literal *Calculus* for setting the Center, and finding the Radius of the Circle that is to intersect the *Parabole* is expressed in readiness for all Cases.

Now *Des Chartes* and all other famous *Analysts* came to miss this general Rule, and himself to fall upon it, he acquaints the Reader in the middle of his Discourse; namely, that they considered the Axe of a *Parabole* and not its Diameter: and affirms, that if it had been his or their hap to have described a Circle from any Point in *Position* given, passing through the *Vertex* of any Diameter in the *Parabole*, and had taken into consideration a certain propriety (than which none could so have suited the design) belonging to the Diameter of any *Parabole*, they could not but with greatest ease, have made a full Discovery of the Universal Rule.

Now whereas in the Title abovesaid, numeral Equations are said to be exemplified; this must be understood only as to their Construction, not as to expressing the value of their Roots in Numbers, about which the Author in a Letter of 24th April last, to Mr. *Collins* saith, that he very well knows when a *Biquadratic* is composed of two *Quadratics*; and hath divers ways to find their Roots in numbers, without seperating them: but he makes not these things his study, in regard he dares undertake to find in numbers all the Roots of any *Cubick* or *Biquadratic* howsoever affected, by aid of his Geometrical Constructions, as soon as any one can by any other way whatsoever: the which he is willing to impart.

Possibly these words may want some Explication, which are added out of a Letter long since communicated by the Learned Mr. *Isaac Newton*, Professor of Mathematics in *Cambridge*, to the aforesaid Mr. *Collins*. Namely, that when a root of any Equation is by any method so near found, that it doth not differ above a tenth part of its self from the true root sought, the residue of the root inquired will be easily calculated by aid of some terms or Fractional parts of an infinite Series or rank of continual Proportionals, derived from the difference between the Resolvend of the known part of the Root, and that whose Root is sought. By which means by raising Resolvends our

out of any assumed Roots with an easy approach, without raising the respective powers of the said Roots, we are delivered from the most toilsom Drudgery of Mathematical Calculations, by finding the Roots of *Æquations in Numbers*, by *Vietas* general method; a thing utterly unknown to the Ancients. However this is not said to disparage that Method which *Vieta* so greatly esteemed, that when he had obtained it, he gave *Algebra* this high *Encomium*, that it did *Nullum non Problema solvere*, in his numerical Method Mr. *Oughtred* and *Harriot* have taken commendable pains. But now last of all, to perform it in Species as Mr. *Isaac Newton* hath done, seems a new Invention never to be sufficiently praised; for out of an *Æquation* of five Dimensions, supposing all the terms extant and affirmed, he hath given a Series for the Root in Species, and such a one as shall serve for finding the Roots of all *Æquations* of 3, 4 or 5 Dimensions, by only altering the signs according as the *Æquation* is affected, and expunging such parts as relate to Deficient terms in an incomplete *Æquation* proposed.

Now that this admirable Doctrine may come to light, and the Learned Author (who hath many other Treatises worthy publick view) may be incited to impart the same, encouragements for the promoting thereof (seeing Undertakers are not to be had without) must be propounded.

It is therefore humbly offered, that the Royal Society by their Treasurer &c. enter into Bond to such Bookseller as shall be the Undertaker, to take of 60 of these Books in Quires at 1 $\frac{1}{2}$ d. each Sheet, and as much each Plate, as soon as printed.

The Treatise it self and the Proposal, is approved and agreed to by the Council of the Royal Society.

And in regard such a Subscription is not sufficient to incite an Undertaker, that the respective Members endeavour by virtue of this Narrative to obtain as many more Subscribers as they can procure amongst others that are not of the Society, each of them to advance half a Crown in hand, in part of the former price: upon which encouragements, *Robert Clavel* Bookseller at the *Peacock* in *St. Pauls-Church-Tard*, is ready to give reciprocal security for the performance according to this Proposal.